1024-17-82 Bojko Bakalov* (bojko_bakalov@ncsu.edu) and Alberto De Sole

(desole@math.harvard.edu). Non-linear Lie conformal algebras with three generators.

The notion of a Lie conformal algebra encodes the commutators of quantum fields in a vertex algebra. Starting from a Lie conformal algebra one can construct a vertex algebra such that the commutators of generating fields are linear combinations of the same fields and their derivatives. The notion of a non-linear Lie conformal algebra captures the general case when the commutators of generating fields involve not only linear combinations but (normally-ordered) products. We classify certain non-linear Lie conformal algebras with three generators, which can be viewed as deformations of the affine Lie algebra $\hat{\mathfrak{sl}}(2)$. We construct free-field realizations of our algebras extending the Wakimoto realization of $\hat{\mathfrak{sl}}(2)$ at the critical level -2. (Received December 31, 2006)