David B. Leep* (leep@ms.uky.edu), Department of Mathematics, University of Kentucky, Lexington, KY 40506-0027. Systems of Quadratic Forms defined over p-adic Fields. Preliminary report.
I will discuss some recent results about solving systems of quadratic forms defined over $p$-adic fields. Let $F_{1}, \ldots, F_{r} \in$ $\mathbb{Z}_{p}\left[x_{1}, \ldots, x_{s}\right]$ be a system of $r$ quadratic forms in $s$ variables with coefficients in the ring of $p$-adic intergers $\mathbb{Z}_{p}, p \neq 2$. Suppose that the reduction modulo $p$ of each quadratic form $a_{1} F_{1}+\cdots+a_{r} F_{r}$ has rank at least $2 r+2$, where each $a_{i} \in \mathbb{Z}_{p}$ and $\left(a_{1}, \ldots, a_{r}\right) \neq(0, \ldots, 0)$. Then the system $F_{1}, \ldots, F_{r}$ has a simultaneous nontrivial zero in $\mathbb{Z}_{p}$. Possible applications and extensions of this result will be discussed. (Received January 08, 2007)

