1025-49-47James Ostrowski* (jao204@lehigh.edu), 27 Memorial Drive West, Bethlehem, PA 18015, and
Jeff Linderoth, Fabrizio Rossi and Stefano Smriglio. Orbital Branching.

We introduce orbital branching, an effective branching method for integer programs containing a great deal of symmetry. The method is based on computing groups of variables that are equivalent with respect to the symmetry remaining in the problem after branching, including symmetry which is not present at the root node. These groups of equivalent variables, called orbits, are used to create a valid partitioning of the feasible region which significantly reduces the effects of symmetry while still allowing a flexible branching rule. We also show how to exploit the symmetries present in the problem to fix variables throughout the branch-and-bound tree. Orbital branching can easily be incorporated into standard IP software. Through an empirical study on a test suite of symmetric integer programs, the question as to the most effective orbit on which to base the branching decision is investigated. The resulting method is shown to be quite competetive with a similar method known as isomorphism pruning and and significantly better than state-of-the-art commercial solvers on symmetric integer programs. (Received January 10, 2007)