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Guido L. Weiss* (guido@math.wustl.edu), Department of Mathematics, Washington University, Box 1146, St. Louis, MO 63130, and **Ilya Krishtal, B Robinson and Edward N Wilson.** *The Construction of Haar Wavelets in Higher Dimensions.*

Orthonormal wavelets in R^n , $n > 1$, are generated by L functions by first translating each by the integral lattice points and then dilating each by the powers of an expanding matrix a in $GL(n, R)$. It is a natural problem to extend the classical Haar wavelet, ψ , and scaling function, ϕ , to this setting. This can be done easily in case $a = 2I$ by appropriate products of these two functions evaluated at each of the n components of the n -dimensional variable x . Such a wavelet is “separable” and has a number of drawbacks. A harder problem is to construct “non-separable” examples associated with more general dilations and translation lattices. Many authors have studied this problem and found Haar-type scaling functions that are characteristic functions of fractal-like sets. We show how one can construct considerably simpler Haar-type wavelets if we use the ideas involved in “composite wavelets.” The latter involve dilations obtained by matrices that are products of the form $(a^j)b$, j an integer, a in $GL(n, R)$ having a “weak” expanding property and b belongs to a subgroup of $GL(n, R)$ having a determinant of absolute value 1. (Received September 11, 2005)