1012-14-73 A Gimigliano and B Harbourne* (bharbour@math.unl.edu), Department of Mathematics, University of Nebraska-Lincoln, Lincoln, NE 68588-0130, and M Ida. Toward a numerical theory for the Betti numbers of ideals of fat points. Preliminary report.

Given multiplicities m_1, \ldots, m_n of general points p_1, \ldots, p_n of P^2 , there is an increasingly well-supported conjecture which, in terms of the m_i only, gives the Hilbert function of the ideal I defining the fat point subscheme $m_1p_1 + \cdots + m_np_n$. No such conjecture for the Betti numbers of the minimal free resolution of I has ever been given. Using a connection between the Betti numbers and splittings of certain rank 2 bundles on P^1 , we give a conjecture for the Betti numbers in many cases. We also formulate a stable version of the problem; our conjecture, it true, would give a complete solution of the stable problem. (Received September 06, 2005)