Meeting: 1006, Lubbock, Texas, SS 2A, Special Session on Differential Geometry and Its Applications

1006-53-119 Emma Carberry* (carberry@math.mit.edu), 2-167 Department of Mathematics, Massachusetts Institute of Technology, Cambridge, MA 02139, and Ian McIntosh and Erxiao Wang. Harmonic maps from the plane to Lie groups and symmetric spaces. Preliminary report.

Harmonic maps from the plane to a compact Lie group or symmetric space form an integrable system, and many such maps can be described in terms of a linear flow on an associated torus \mathbb{C}^g/Λ . This torus is the Jacobian of an algebraic curve X, called the spectral curve. This point of view introduces an important invariant of the harmonic map, namely its spectral genus g = genus(X). The spectral genus gives the dimension of the space of deformations of the harmonic map, and in some geometrically interesting cases provides a lower bound for its energy. We shall describe how, in several situations, studying the spectral genus has led to the proof of the existence of arbitrarily large families of minimal 2-tori. In particular, we shall describe some such work of relevance to mirror symmetry and to M-theory. (Received February 10, 2005)