Meeting: 1001, Evanston, Illinois, SS 12A, Special Session on Iterated Function Systems and Analysis on Fractals

1001-26-54 Ka-Sing Lau* (kslau@math.cuhk.edu.hk), Dept. Math., The Chinese Univ. of Hong Kong, Hong Kong, Peoples Rep of China, and King Shun Leung, Math. Dept., Hong Kong Inst. of Education, Hong Kong, Peoples Rep of China. On the Connectedness and Disklikeness of Self-affine Tiles. Preliminary report.

There is very limited knowledge about the connectedness of self-affine tiles T in \mathbb{R}^n . In here we consider the case that T is generated by an $n \times n$ integral expanding matrix A with det A = q and a consecutive collinear digit set of the form $\mathcal{D} = \{0, v, \dots (|q| - 1)v\} \in \mathbb{Z}^n$. In \mathbb{R}^2 , T is always connected; by using a criterion of Bandt and Wang, we show that T is disklike if and only if $2|p| \leq |q+2|$ where $x^2 + px + q$ is the characteristic polynomial of A. For higher dimension the connectedness problem become more complicated, we settle this in \mathbb{R}^3 but the question remains open in general. (Received July 27, 2004)