Meeting: 1001, Evanston, Illinois, SS 24A, Special Session on Hopf Algebras at the Crossroads of Algebra, Category Theory, and Topology

1001-16-274Robert L. Grossman and Richard G. Larson* (rgl@uic.edu), MSCS m/c 249, Univ. of
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The vector space spanned by labeled rooted trees forms a Hopf algebra. Let k be a field and let R be a commutative k-algebra. Let H denote the Hopf algebra of rooted trees labeled using derivations of R. We introduce a construction which gives R a H-module algebra structure and show this induces a differential algebra structure of H acting on R. We describe how certain actions of H on R are determined by the actions of derivations E of R, and by $\nabla_E F$, where E, F are derivations of R, and ∇ is the (Koszul) connection. This work extends the notion of a R/k-bialgebra introduced by Nichols and Weisfeiler. (Received August 29, 2004)