Meeting: 1001, Evanston, Illinois, SS 1A, Special Session on Modern Schubert Calculus

1001-14-141 Ravi Vakil* (vakil@math.stanford.edu), Department of Mathematics, Stanford University, Stanford, CA 94305. Monodromy and Galois groups of Schubert problems.

Enumerative problems in geometry often have groups attached, which have different interpretations in geometry, arithmetic, and algebra. The geometric interpretation is as follows: if the problem has N solutions, and the conditions are moved about and returned to their starting positions, how can the N solutions be permuted? Schubert problems are the only known enumerative problems that can have unexpectedly small Galois groups; the first such example is due to Derksen. By solving Schubert problems over the rational numbers (and using Schubert induction) we can compute these monodromy groups explicitly; we give examples where it is the full symmetric group, and where it seems to be mysteriously small. This is part of a larger project with Sara Billey. (Received August 20, 2004)