

**Meeting:** 1001, Evanston, Illinois, SS 9A, Special Session on Solving Polynomial Systems

1001-12-121      **Christopher J Hillar\*** ([chillar@math.berkeley.edu](mailto:chillar@math.berkeley.edu)), Dept. Mathematics, University of California, Berkeley, Berkeley, CA 94720. *Reconstructing dynamical systems from their zeta functions.*

The  $m$ -th cyclic resultant of a polynomial  $f \in \mathbb{C}[x]$  is

$$r_m = \text{Res}(f, x^m - 1).$$

We characterize polynomials having the same set of nonzero cyclic resultants. Sequences of the form  $r_m$  arise (among many other places) as the cardinalities of sets of periodic points for toral endomorphisms. Let  $f$  be monic of degree  $d$  with integral coefficients and let  $X = \mathbb{T}^d = \mathbb{R}^d/\mathbb{Z}^d$  denote the  $d$ -dimensional additive torus. Then, the companion matrix  $A_f$  of  $f$  acts on  $X$  by multiplication mod 1; that is, it defines a map  $T : X \rightarrow X$  given by

$$T(\mathbf{x}) = A_f \mathbf{x} \bmod \mathbb{Z}^d.$$

Let  $\text{Per}_m(T) = \{\mathbf{x} \in \mathbb{T}^d : T^m(\mathbf{x}) = \mathbf{x}\}$  be the set of points fixed under the map  $T^m$ . Under the ergodicity condition that no zero of  $f$  is a root of unity, it turns out that  $|r_m(f)| = |\text{Per}_m(T)|$ . We describe how our results allow for reconstruction of such dynamical systems from their zeta functions,

$$Z(T, z) = \exp \left( - \sum_{m=1}^{\infty} |\text{Per}_m(T)| \frac{z^m}{m} \right).$$

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