

Meeting: 1001, Evanston, Illinois, SS 12A, Special Session on Iterated Function Systems and Analysis on Fractals

1001-11-352 **David Applegate**, 180 Park Avenue, Building 103, Florham Park, NJ 07932-0971, and **Jeffrey C Lagarias*** (lagarias@umich.edu), Dept. of Mathematics, University of Michigan, Ann Arbor, MI 48109. *The $3x+1$ Semigroup*. Preliminary report.

Let S be the multiplicative semigroup generated by 2 and the positive rational numbers of form $(2n+1)/(3n+2)$, for nonnegative integers n . We consider the question: Which integers belong to S ? This problem was raised by Herschel Farkas, and represents a weakened form of the $3x+1$ problem, in that the backwards $3x+1$ iteration can be encoded in terms of generators of S . The (unproved) $3x+1$ Conjecture implies that all positive integers should belong to S . We prove unconditionally that this is the case. In doing so we obtain a complete description of S . (Received August 31, 2004)