Meeting: 999, Nashville, Tennessee, SS 3A, Special Session on Index Theory and the Topology of Manifolds

999-57-202 Bruce Williams* (williams.4@nd.edu), Dept. of Mathematics, 255 Hurley Hall, Notre Dame, IN 46556-4618. Family Version of Surgery Theory.

(joint with Michael Weiss) Suppose $p: E \to B$ is a fibration with fibers n-dim. Poincare complexes, n > 4, and B a compact CW complex of dimension q.

Question: When is p fiber homotopy equivalent to a fiber bundle with fibers closed n-dim. topological manifolds?

When B is a point, Ranicki's total surgery obstruction theory implies the answer is yes iff the visible symmetric signature of E can be lifted to the domain of a certain assembly map. If B is general but we weaken fiber bundle to "block bundle", then Quinn's thesis implies the answer is yes iff the fiberwise visible symmetric signature of p has a fiberwise lifting to an assembly map.

We define a certain refined fiberwise visible symmetric signature of p such that if the answer is yes, then our refined invariant has a fiberwise lifting to an assembly map. We also get a converse when 3q < n-6. (Received August 23, 2004)