Meeting: 1002, Pittsburgh, Pennsylvania, SS 2A, Special Session on Convexity and Combinatorics

1002-52-49 Marilyn Breen* (mbreen@ou.edu), Department of Math, University of Oklahoma, 601 Elm Avenue, Norman, OK 73019. Helly-type theorems for intersections of starshaped sets.
Some familiar results for intersections of convex sets may be extended to intersections of starshaped sets. Among the results are the following: Let $k$ and $d$ be fixed integers, $0 \leq k \leq d$, and let $\mathbb{S}$ be a collection of sets in $\mathbb{R}^{d}$. If every countable subfamily of $\mathbb{S}$ has a starshaped intersection, then $\cap\{S: S \in \mathbb{S}\}$ is (nonempty and) starshaped as well. If every countable subfamily of $\mathbb{S}$ has as its intersection a starshaped set whose kernel is at least $k$-dimensional, then the kernel of $\cap\{S: S \in \mathbb{S}\}$ is at least $k$-dimensional, too. (Received July 26, 2004)

