Meeting: 1002, Pittsburgh, Pennsylvania, SS 2A, Special Session on Convexity and Combinatorics

1002-52-21 Margaret M. Bayer* (bayer@math.ku.edu), Department of Mathematics, University of Kansas, 405 Snow Hall, 1460 Jayhawk Blvd., Lawrence, KS 66045-7523. Reconstruction of polytopes as Eulerian posets. Preliminary report.
Results on combinatorial reconstruction for polytopes are of the following form: If $P$ and $Q$ are convex $d$-polytopes, $P$ is in a specified class (e.g., simplicial polytopes, simple polytopes, zonotopes), and the $k$-skeletons of $P$ and $Q$ are combinatorially equivalent, then $P$ and $Q$ are combinatorially equivalent. (The $k$-skeleton is the subcomplex of the boundary complex consisting of all faces of dimension at most $k$.) In this talk we consider what happens if we relax the hypothesis on $Q$, requiring only that $Q$ be an Eulerian partially ordered set. We show that if $P$ is a simplicial $d$-polytope, then the face lattice of $P$ is the unique Eulerian poset agreeing with $P$ on all but the dimension $r$ faces of $P$, for $0 \leq r \leq d-2$, and give a counterexample for $r=d-1$. (Received June 29, 2004)

