

Meeting: 1002, Pittsburgh, Pennsylvania, SS 8A, Special Session on Graph Polynomials

1002-05-23 **David G. Wagner*** (dgwagner@math.uwaterloo.ca), Department of C&O, University of Waterloo, Waterloo, Ontario N2L 3G1, Canada. *A strange tree–enumeration formula from electrical network theory.*

For a graph $G = (V, E)$, let $y := \{y_e : e \in E\}$ be indeterminates and let $G(y) := \sum_T y^T$ with the sum over all spanning trees of G , where $y^T := \prod_{e \in T} y_e$. For $e, f \in E$, let G_e^f denote G with e contracted and f deleted, *et cetera*. In her thesis, Y.-B. Choe gave two proofs that there is a polynomial $C(G, e, f; y)$ such that

$$G_e^f(y)G_f^e(y) - G_{ef}(y)G^{ef}(y) = C(G, e, f; y)^2.$$

In fact $C(G, e, f; y)$ is a signed enumerator for certain two–component forests in G . This formula is a standard result in electrical network theory, being a sharp statement of the Rayleigh monotonicity property. One of Choe’s proofs (based on that of Feder and Mihail) generalizes to sixth–root of unity matroids. The challenge I pose to the audience is to find a combinatorial (bijective) proof of this formula. (Received July 06, 2004)